

PROBLEM OF PREDICTING THE SPREAD OF CORONAVIRUS (COVID-19) FOR THE WORLD

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Abstract

It is well known, that the recent spread of the Coronavirus COVID-19 has become a vital problem for the whole world. Suffice it to say that it was declared a pandemic by the World Health Organization on March 11 this year. Therefore, it is understandable what the significance of the problem of predicting its spread may be. This work is dedicated to the experience and results of our research in this regard.

For clarity, we have note, that we discussed the forecasting problem for such characteristics of spread of the virus as the total number of infections worldwide (total cases) and the number of active cases (active cases).

Predictive estimates of these indicators have been found by us since February 13. However, given that the virus (originally spreading in China) spread around the world, that is, its spread has dramatically changed and, in addition, most of our prediction models have been short-lived, periodic adjustments to our prognostic estimates have been necessary.

However, it should be noted that the prognostic estimates we initially found (based mainly on the spread of the virus in China) were quite accurate. Specifically, according to our forecast, by the end of March, the total number of people infected with the virus should not have exceeded 85,000, actually in China (which actually defeated the virus!), as of March 21, amount of infected is 81008.

Keywords: Coronavirus, Prediction, Prediction Models, Predictive Validity.

1. Introduction

Recently, the spread of coronavirus COVID-19 has become a vital problem for the whole world. Suffice it to say that it was declared a pandemic by the World Health Organization on March 11 this year. Therefore, it is understandable what importance can be attached to the problem of predicting its prevalence. The results and experience of our research in this regard will be described below.

2. Presentation of the main research material

For certain, it should be noted that in terms of our prediction, we considered the main indicators of the spread of coronavirus, such as the total number of cases of infection (in the world) for the current time (**total cases**), which is described below with the variable $infic$ and the number of active cases (i.e. infected with this virus) for the current moment (**active cases**), which is denoted below by the variable ac . (Understandably, the difference between these two values is the total number of patients who have recovered and died (worldwide).)

Initially we tried to predict the values of the $infic$ variable in the database for the period 22 / 01-13 / 02 2020 (in days), for the period 13 / 02-29 / 02. Therefore, it is clear that the data of February 13 were used by us in the so-called ex post forecasting or for selecting a forecasting model.

It is interesting to note that based on the characteristics of these models (at the first stage) and the data of February 13, we considered the most reliable model of forecasting the Ferhulsts logistic growth model [Verhulst, 1845 :1-45], whose general appearance looks like this

$$P(t) = \frac{K_0}{(K - P_0)e^{-rt} + P_0}, \quad (1)$$

where P_0 denotes the number of population (in this case infected) at the initial moment, and K is the maximum number of population (in this case infected).

It should be noted that during this period the virus was mainly spread in China and the data were mainly consistent with its spread in China.

In this case, taking into account the data of February 13, we took the value of the K parameter equal to 85000 (which in this case turned out to be quite accurate, considering that this figure was 85214 as of September 15!) (I.e. within 7 months forecasting Error with real value, only 0.25% came out !!)

So the magnitude of the maximum rate of increase, r , in this case we were looking for from the following equation of regression (it should be noted that all our basic calculations were performed on the basis of the well-known computer program EViews-10 [Gabelaia A., Gabelaia L. 2017:433 p.]:

$$INFIC = (85000 * 580) / ((85000 - 580) * \text{EXP}(-C(1) * @TREND) + 580).$$

The value of the r parameter obtained as a result of this regression was $r = 0.279355$. However, the determination coefficient of this regression was in the order of 0.93, with a very high (equal to 59.2) t -statistic, only the Durbin-Watson statistic came out very small, indicating that the regression may be characterized by systematic errors. In addition, a diagram of its error gives some idea of the accuracy of this model (see Fig. 1)).

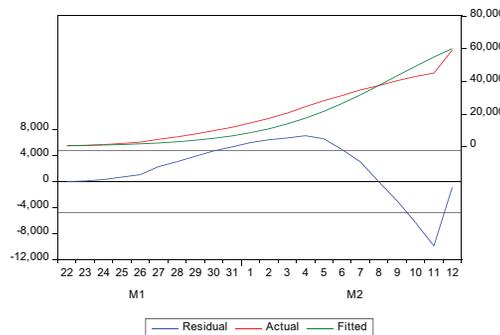


Fig.1. Error diagram of the logistics model of infection

As for the predictive estimates of infic magnitude based on this model and their ratio to the actual values of this magnitude for a given period, is shown in Figs. 2, where infic and infic1, respectively, indicate the actual magnitude of the number of infected and its (pre-) forecast.

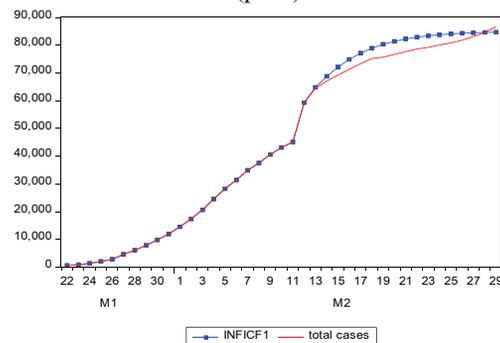


Fig.2. Dynamics of prognostic and real indicators of infection
For the period 13 / 02-29 / 02 2020

A more accurate representation of the error of the obtained predictive estimates is given by the $cdomf1=inficf1-infic$ histogram of its error and the statistical characteristics shown in Figs. At 3 p.m.

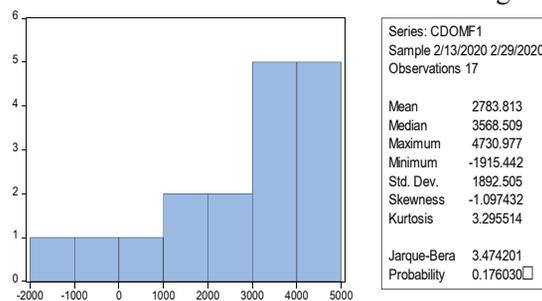


Fig.3. Histogram and statistical characteristics of error in predictive estimates of infection

As we can see, the forecasting results at this **(first) stage** are not so bad (the mean error and standard deviation for the forecasting period were 2784 and 1593 units, respectively).

We can be sure that the so-called the mean error of the approximation (percentage of the modulus of error relative to the real values), which in this case is calculated by the formula

$$A = \left(\frac{1}{n} \sum_{i=1}^n \left| \frac{inf icf1_i - inf \dot{e}_i}{inf \dot{e}_i} \right| \right) * 100\%$$

(where n denotes the length of the forecast horizon)

amounted to 3.3%!

It should be noted that gradually, after the virus has crossed the borders of one country, the dynamics of its spread has significantly deviated from the form of the logistic curve used above (which, as mentioned above, allows for relatively long-term forecasting!) and demanded more complex, e.g. use of ARIMA (Integrated Models of Autoregression and moving average (which is visually well visible on the actual virus distribution graphs). However, the disadvantage of these models is that they usually give short-term forecasts!

In particular, **in the second stage**, we tried to predict the total number of infected people for the month of March, based on the data already in January-February (more precisely, 22 / 01-29 / 02 2020), based on the already mentioned ARIMA type models.

The trend model of the $infic$ variable, with an autoregressive member, for this period took the form:

$$INFIC = 2419.82056382 * @TREND + [AR(1)=0.934518885427, UNCOND, ESTSMPL="1/23/2020 2/29/2020"]. \quad (2)$$

It should be noted that the coefficient of determination of this regression came out very high (in the order of 0.99), the t-statistics of the parameters were equal to 6.4, 10.8 and 5.8, respectively, only the Durbin-Watson statistics came out a little low (in the order of 1.26), which suggests that regression is not insured against systematic errors. Clearly, the diagram of its error also gives some idea of the accuracy of this model (see Fig. 4)).

As for the predictive estimates of $infic$ magnitude based on this model and their ratio to the actual values of this magnitude based on the March 1-15 data shown in Figs. 5, where $infic$ and $inficf2$, respectively, indicate the actual number of infected and its (pre-) forecast.

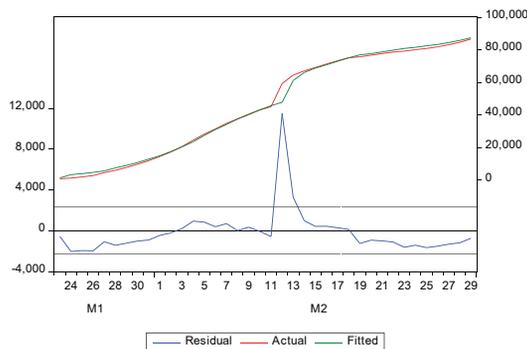


Fig.4. Infection (2) model error diagram

As we can see, the accuracy of the prediction deteriorated rapidly from March 11, when the virus spread to virtually the entire world. Naturally, these dramatic changes, in the area and conditions of the spread of the virus, greatly complicated the problem of its prediction, especially since we here usually use passive prediction methods based on the assumption that the future should look like the past. This explains the circumstance that below we were forced to do the so-called optimistic and pessimistic forecast estimates that differed significantly from each other.

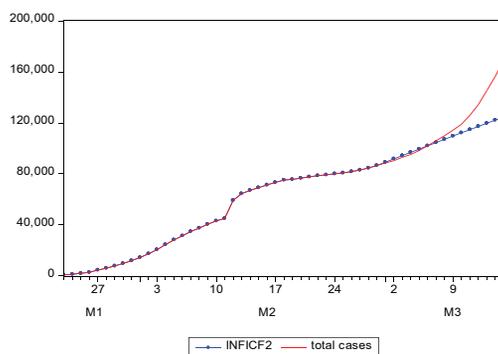


Fig.5. Dynamics of prognostic and real indicators of infection
For the period 1 / 03-15 / 03 2020

Therefore, we made the decision to adjust our forecast estimates from March 11 this year.

As for the accuracy of the forecast estimates we received for the first decade of March, the average error of its approximation was 2%!

It should be noted that the average error in the approximation of the predicted estimates of the infic variable obtained from similar models above was 2.8% for the second decade of March!

Based on all the above (already in the fourth stage!), we made forecasts for the third decade of March, for which the average approximation error was 1.75%!

In addition, as the relevant calculations show, for the period 13 February-31 March, the weighted average error of the approximation of our forecasts was 2.57%!

In the fifth phase, the average error in the approximation of the prognostic assessment of infection for the first half of April was 2.14%.

In the sixth phase, ie in the second half of April, the average error in the approximation of forecast estimates was 1.7%.

In the seventh stage, ie in the first half of May, the average error in the approximation of our forecast estimates was 0.54%.

In the eighth phase, for the period May 16-June 15, the average error in the approximation of our forecast estimates was 0.9%.

In the ninth phase, i.e. for the second half of June, the average error in the approximation of our forecast estimates was 2.73%.

In the tenth phase, the average error in the approximation of our forecast estimates for the first half of July was 2.23%.

At the eleventh stage, i.e. in the second half of July, the average error in the approximation of our forecast estimates was 1.2%.

In the twelfth stage, i.e. in August the average error in the approximation of the forecast estimates was 2.15%.

Finally, the dynamics of the main characteristics of the spread of the virus to the world (in terms of days) between January and August 2020 looked like this (see Figure 6-9):

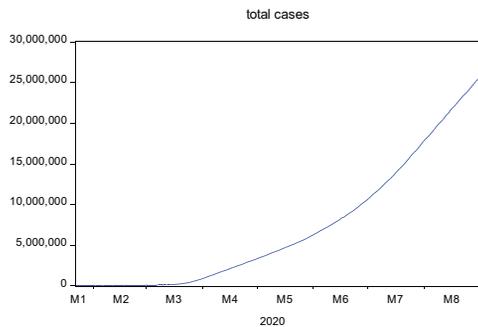


Fig.6. Dynamics of the number of infected (infc) in the period January-August 2020 (in terms of days)

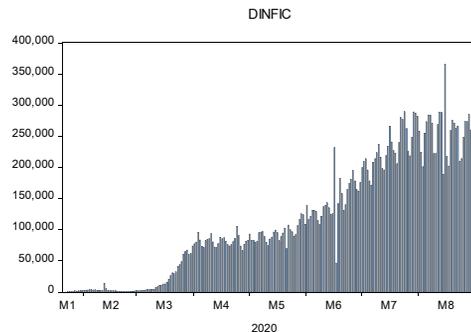


Fig.7. Dynamics of the growth rate of the number of infected people (d(infc)) in the period January-August 2020 (in terms of days)

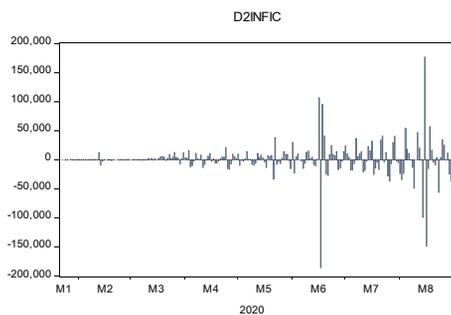


Fig.8. Dynamics of „acceleration“ of the growth of the number of infected people (d(infc, 2)) in the period January-August 2020 (in terms of days)

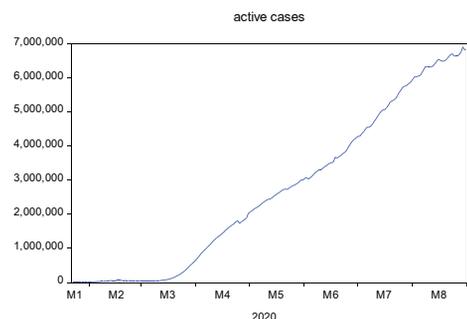


Fig.9. Dynamics of the number of patients with the virus (ac) in the period January-August 2020 (in terms of days)

As we can see, the forecasting models we use (which are known to work well in the short run!) Show really high enough accuracy for a maximum of a month (then their accuracy drops!). On the other hand, the virus is „not going to stop“ in the near future, which calls into question the prospects of using the above

prediction methods. Therefore (in order to increase the forecasting horizon!), It may make sense to consider a new indicator such as e.g. „Average daily increase in the number of infected people per month“, which will allow us to make a forecast of this figure for a horizon of several months, which we are going to do in the future!

Therefore (in order to increase the forecasting horizon!), It may make sense to consider a new indicator such as e.g. „Average daily increase in the number of infected people per month“, which will allow us to make a forecast of this figure for a horizon of several months, which we are going to do in the future! Moreover, according to the central limit theorem, the distribution of this indicator should be close to normal, which will simplify the task of finding reliable predictive estimates for it.

In particular, the dynamics of this indicator for the world in January-October 2020 looked like this:

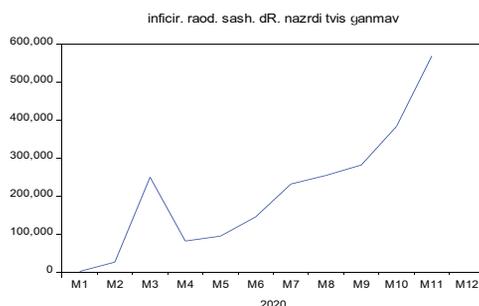


Fig.10. Average daily increase in the number of infected dynamics in the world with January-October 2020 data

Conclusion

As we can see, in the given period this indicator (if we do not count the local maximum in March) was developing in an ascending line, i.e. the spread of the virus in the world had a permanently upward dynamics, although this growth was not as avalanche-like in Georgia as it has been in the last two months.

It should be noted that as for the mortality rate caused by this virus (percentage of deaths to the total number of survivors and deaths), it initially increased rapidly enough to 21%, but then slowly dropped to 3% (as of the end of October!). However, we must bear in mind that above we talked about the cumulative (accumulated) value of this indicator! As for its current importance (since „critical“ make up only 1% of the current number of patients), we must assume that the current mortality rate for this virus is even lower. However, unfortunately, it is characterized by a very high speed of propagation.

References

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